

# ESGI

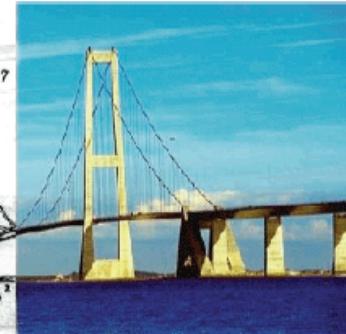
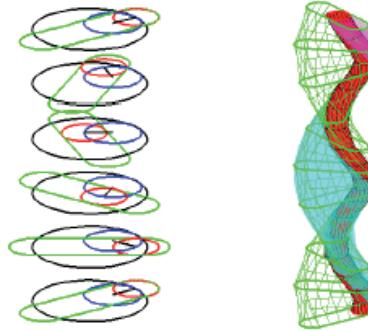
European Study Group  
with Industry

$$y_{min} = 77$$
$$y_{max} = 254$$
$$P(x) = 2,68 \cdot 10^{-4} x^2 + 77$$
$$C: x^2 + (y - 44.928)^2 = 15000^2$$



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$$\begin{aligned}
 &= \frac{1}{2} \int \frac{1+z}{z\sqrt{1+z^2}} dz = \frac{1}{2} \\
 &= \int \frac{dz}{z\sqrt{1+z^2}}, z = I/J \\
 &\cdot \int \frac{-dt}{t^2} = \\
 &\sqrt{\frac{1}{t} \sqrt{1+\frac{1}{t^2}}} = 
 \end{aligned}$$



# EUROPEAN STUDY GROUPS WITH INDUSTRY

## 1-uges Arbejdsmøde

*European Study Groups with Industry*, (ESGI) er et 1-uges arbejdsmøde hvor matematikere takler konkrete matematiske problemstillinger fra virksomheder.

Hver virksomhed bringer en opgave til mødet.

Ved mødets begyndelse (mandag) præsenterer virksomhederne opgaverne.

Matematikerne arbejder herefter intensivt i grupper på at løse opgaverne.

Ved mødets slutning (fredag) præsenteres løsningerne for virksomhederne, og efterfølgende leveres en rapport til virksomheden.

I Danmark ligger mødet hvert år i august måned, enten på DTU (Kgs. Lyngby) eller på SDU (Odense/Sønderborg).

## Pris

Hver deltagende virksomhed betaler DKK 25.000 for deltagelse.

Virksomheden bedes derudover have en repræsentant til rådighed for arbejdsguppen, så stor en del af ugen som muligt.

## Arbejdsmødet giver

- \* input fra modelleringsekspertter
- \* fokusering af problemstillinger
- \* brainstorm på løsningsmuligheder
- \* adgang til de nyeste teoretiske og beregningsmæssige teknikker

## Erfaringer

ESGI arbejdsmøder har være afholdt i Danmark i over 10 år. Virksomheder som NOVO-Nordisk, Danfoss, Grundfos, Danisco, DSB, Danske Bank, DONG Energy, og mange mindre, også helt små, firmaer har deltaget.

Deltagende virksomheder har

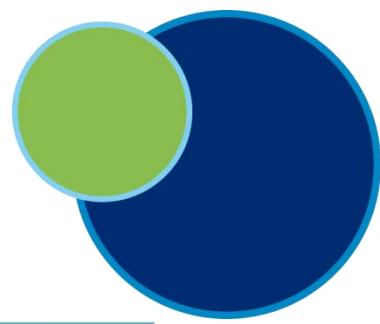
- \* Fundet eksplisitte løsninger
- \* Fundet nye modeller af komplicerede problemstillinger
- \* Etableret kontakter til forskere
- \* Etableret kontakter med ph.d. studerende



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## European Study Group with Industry



**ESGI: Få en gruppe af forskere til at arbejde for din virksomhed  
- ganske gratis**



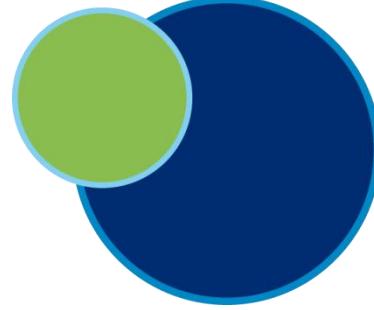
Som medlem af VE-Net har du nu mulighed for ganske gratis at få stillet et panel af ingeniører, fysikere og matematikere til rådighed for din virksomhed i en uge. Har din virksomhed en problemstilling af matematisk karakter, som I ikke selv vil kaste jer over – så er European Study Group with Industri (ESGI) måske noget for jer. Både små og store virksomheder er velkomne.

ESGI finder i år sted:

Mandag d. 15. - fredag d. 19. august 2010  
på Syddansk Universitet i Sønderborg



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## Problem example 1

### Danfoss PolyPower



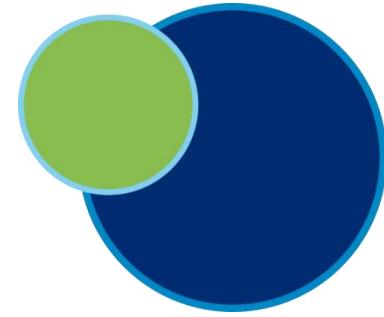
### Peristaltic hydraulic pump based on DEAP materials

- 11 Researchers

DTU, SDU (MMMI, MCI), Univ. of Southampton, Danfoss.

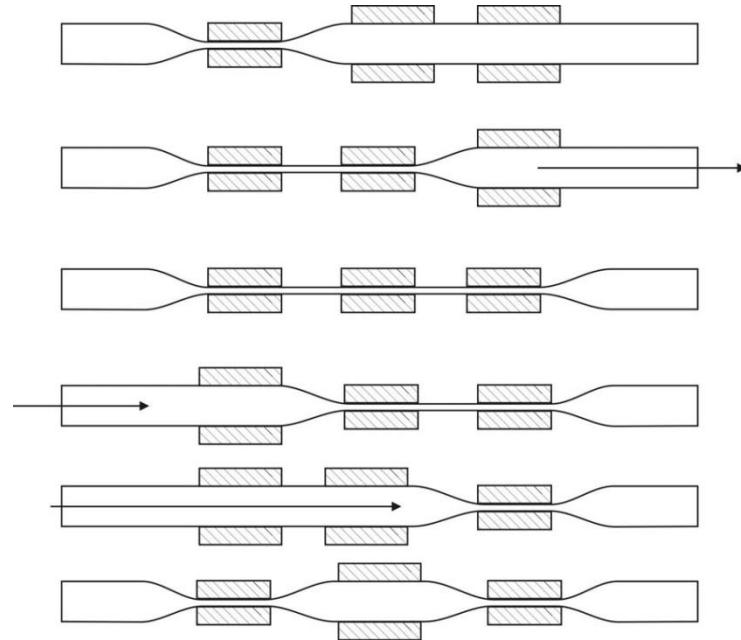
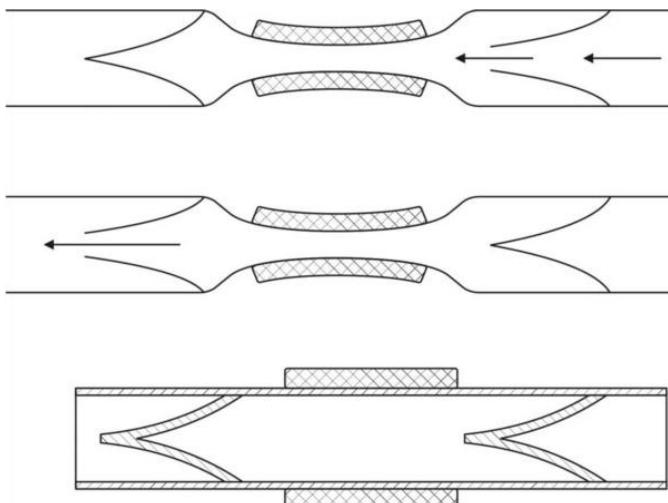
- Solution report (22 pages) with 3 different approaches and consideration of travelling waves and stacking of pumps
- Specific model build – Intensive work and sparring

# ESGI... Danfoss PolyPower



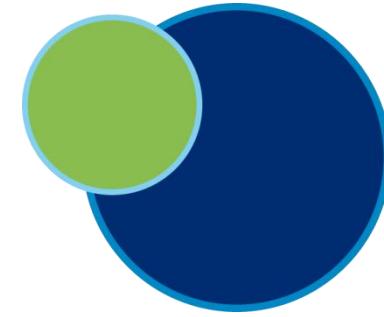
## Background

The basic idea is to develop a peristaltic pump based on the Danfoss PolyPower Technology



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# Danfoss PolyPower



## Problem statement

Please consider the problematic and propose a viable and efficient design based on optimal efficiency.

Pump specification:

- Volume flow: 2.2 m<sup>3</sup>/h
- System pressure: 10 bar
- Pipe diameter: 1/2 inch

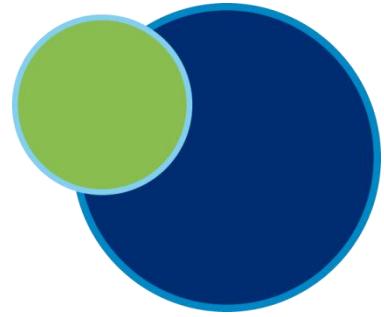
- Lift: 4 m water column (0.4 bar)
- Max length of pump: 180 mm

How efficient a design I achievable? The system may be run at mechanical and electrical resonance.

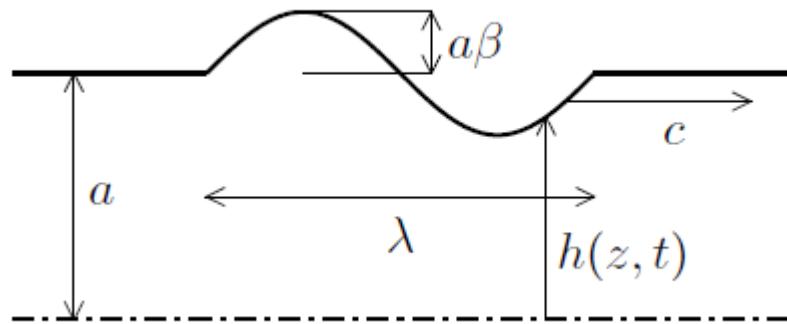
A number of reasonable models describing the PolyPower actuator as a mass/spring/damper system exist.

BR  
Frands Voss  
Danfoss Ventures A/S, 2010-08-12

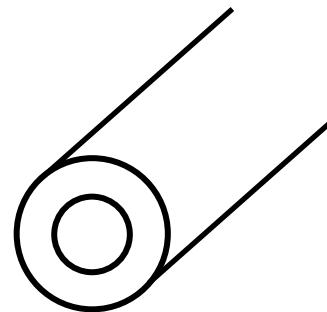
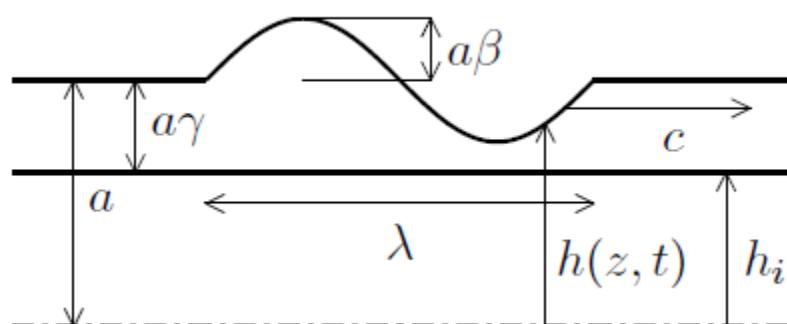
# ESGI... Danfoss PolyPower



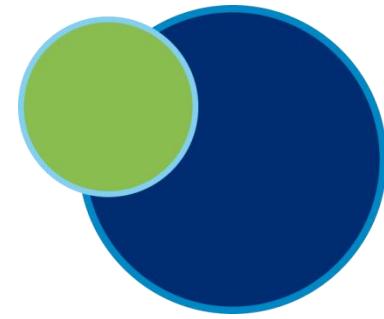
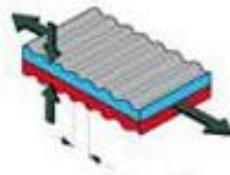
## Solution



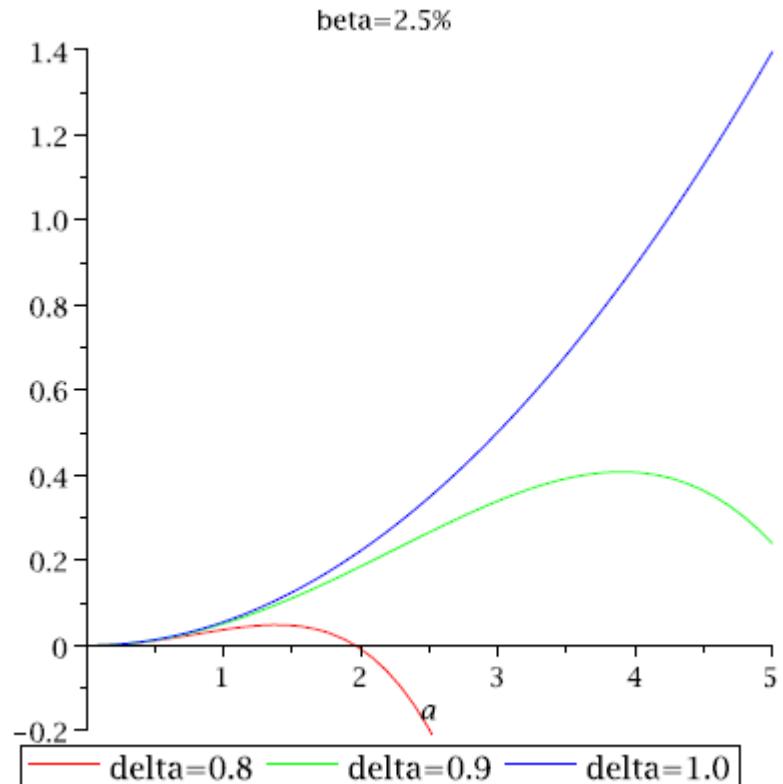
$$2\pi h \frac{\partial h}{\partial t} + \frac{\partial Q}{\partial z} = 0,$$



# ESGI... Danfoss PolyPower

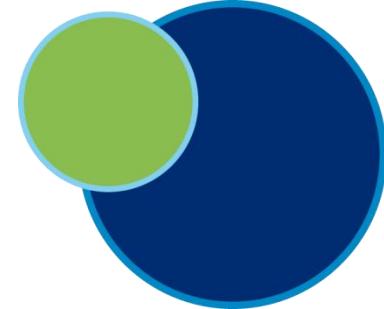


## Solution



# ESGI...

## Danfoss PolyPower



### Danfoss Problem: Peristaltic Pumping Using Polymer Materials

Andreas Rune Fugl<sup>1</sup>, Niels Fuglede<sup>2</sup>, Jens Gravesen<sup>2</sup>,  
Michael Pilegaard Hansen<sup>2</sup>, Peter Røgen<sup>2</sup>, Jens Starke<sup>2</sup>,  
Mads Peter Sørensen<sup>2</sup>, Colin Please<sup>3</sup>, Frands Voss<sup>4</sup>,  
Morten Willatzen<sup>5\*</sup>; Lin Xiao<sup>5</sup>

<sup>1</sup>Mads Clausen Institute and Maersk Institute, University of Southern Denmark

<sup>2</sup>Department of Mathematics, Technical University of Denmark

<sup>3</sup>Faculty of Mathematical Studies, University of Southampton

<sup>4</sup>Danfoss A/S

<sup>5</sup>Mads Clausen Institute, University of Southern Denmark

September 30, 2010

The Danfoss problem was split up in different subgroups where different subproblems were tackled. These include (a) a low Reynolds number one-dimensional analytical analysis for a cylindrical pipe and an annulus, (b) actuator stacking configurations, (c) a two-dimensional analysis of the low (or, actually zero) Reynolds number problem, (d) the high Reynolds number problem, and (e) a FEM analysis using the software COMSOL. The different treatments are described in the following.

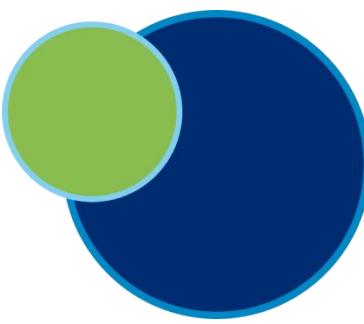
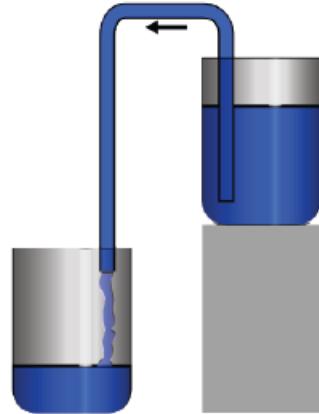


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## Problem example 2

### DHI Group

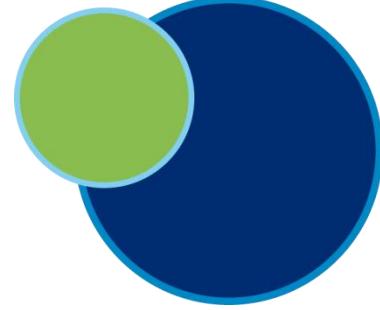
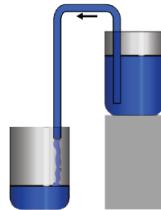


### Design parameters for a siphon system

- 10 Researchers
  - DTU, SDU, TU Eindhoven, Univ. of Southampton, Polish Acad. Sci. Warsaw, U. Oxford, DHIVand.
- Solution report (16 pages) with 5 different approaches, including electrical analogy and extension with groundwater effects
- Specific model build – Intensive work and sparring

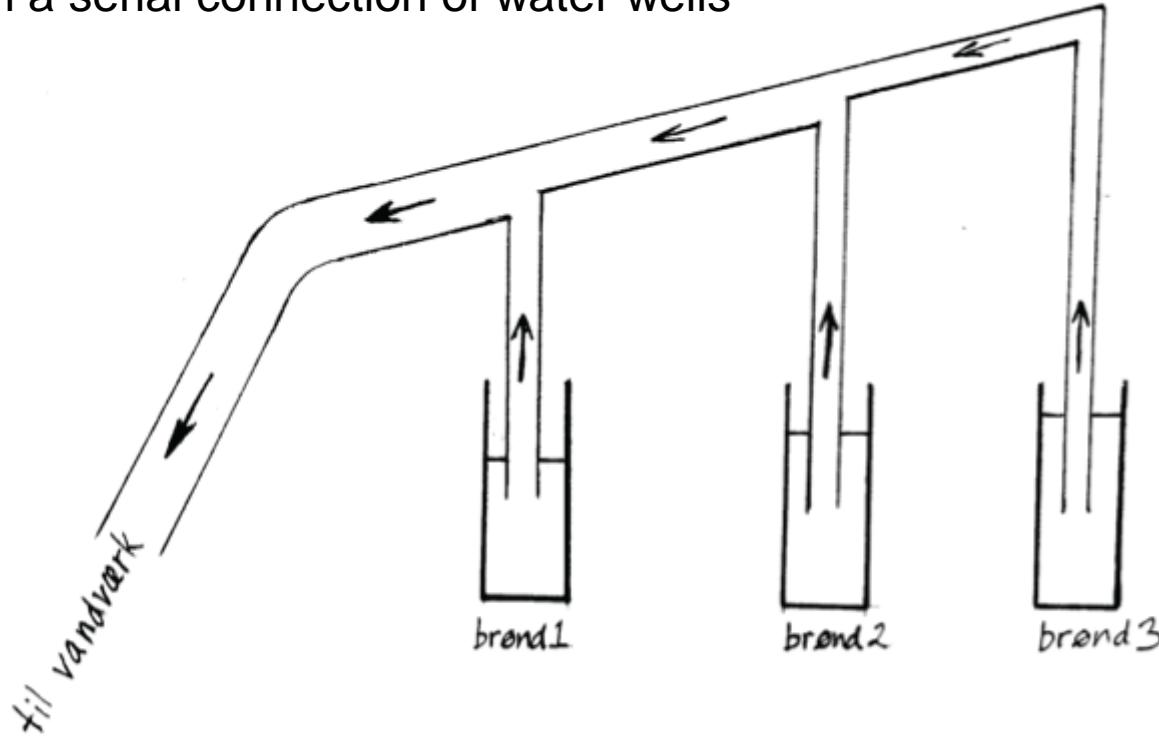
# ESGI...

## DHI Problem



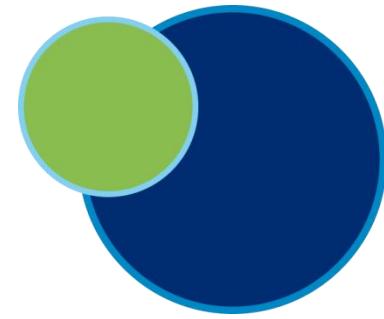
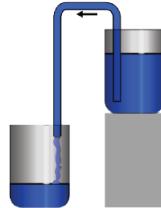
## Background

The idea is to utilize the siphon principle in extraction of groundwater from a serial connection of water wells



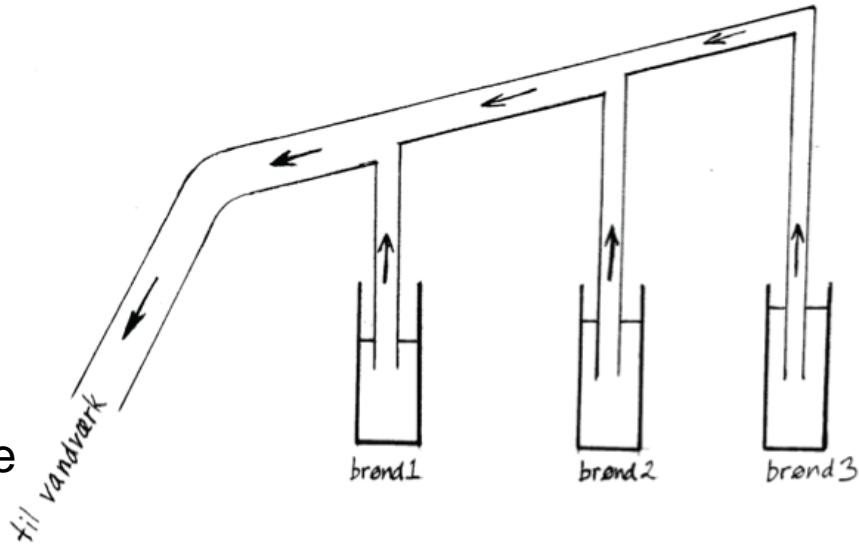
# ESGI...

## DHI Problem



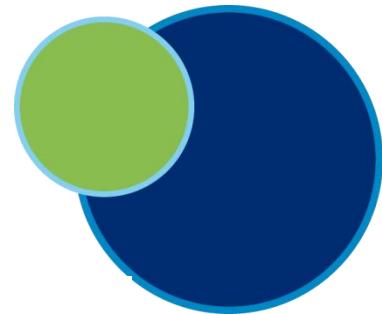
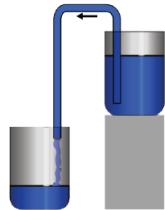
### Problem statement

- What parameters in this system will determine the flow distribution from the wells?
- How will the water table in the wells influence the flow?
- How will pipe dimensions determine the flow?
- Can water go from one well to another?
- Where in the system is the greatest risk of cavitation?

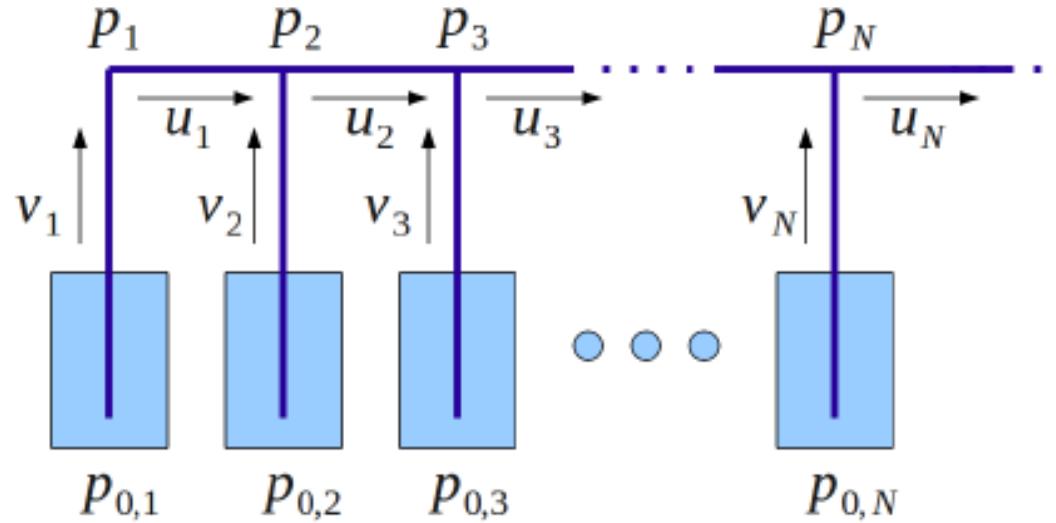


# ESGI...

## DHI Problem



### Solution



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$$v_j |v_j| = p_j - p_{0,j} \quad u_j |u_j| = p_{j+1} - p_j \quad u_{j+1} = u_j + v_j$$

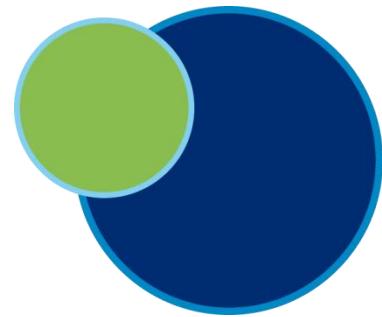
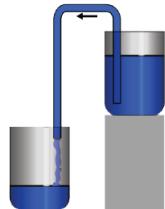
$$\frac{d(A(x)u)}{dx} = B(x)v \quad \text{for } 0 \leq x \leq L .$$



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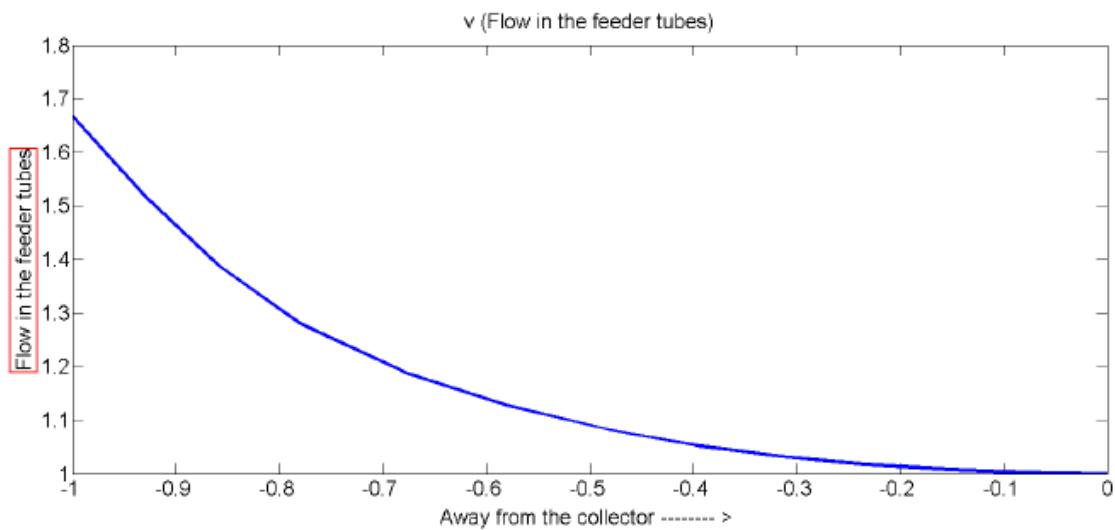
## DHI Problem



## Solution

$$A \propto (L - x)^{\frac{4}{5}}.$$

Samlerrør v. ens brøndbelastning

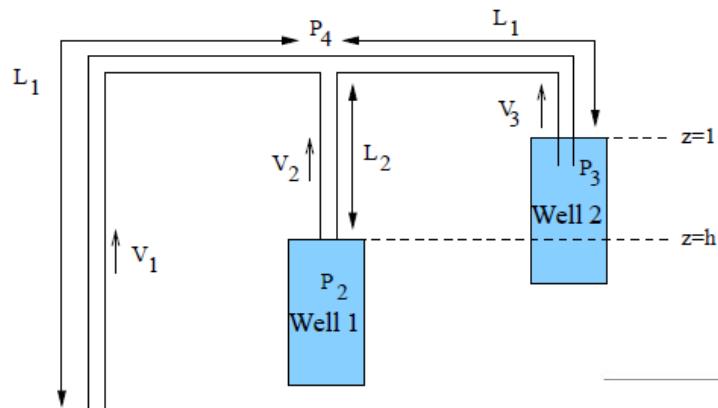
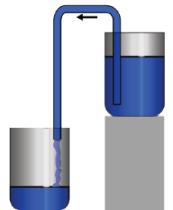


Flow i samlerrør v.  
ens brønd-niveau

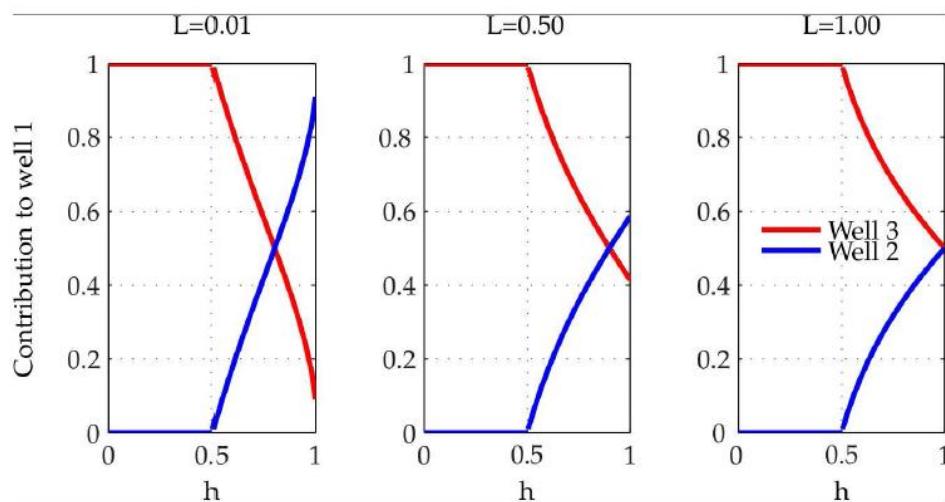


# ESGI...

## DHI Problem

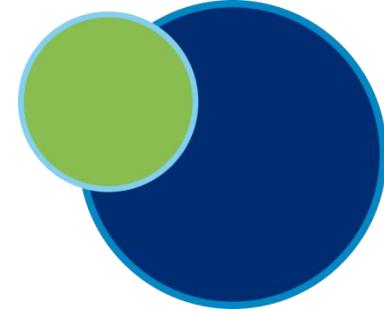
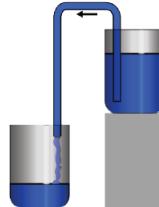


$$\frac{L_2}{L_1} = L$$



# ESGI...

# DHI Problem



## Design Parameters for a Siphon System

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Jørgen Sylvest (USD, Odense), Kundan Kumar (TUE, Eindhoven),  
Maria Rudnaya (TUE, Eindhoven), Valeriu Savcenco (TUE, Eindhoven),  
Borys Sobiegraj (Polish Acad. Sci., Warsaw), Colin Please (U. Southampton),  
Rob Style (U. Oxford)

Problem Presenter: Anne Katrine Falk (DHIVand MiljøSundhed, Hørsholm )

76th EUROPEAN STUDY GROUP with INDUSTRY

Department of Mathematics  
Technical University of Denmark  
16 - 20 August 2010

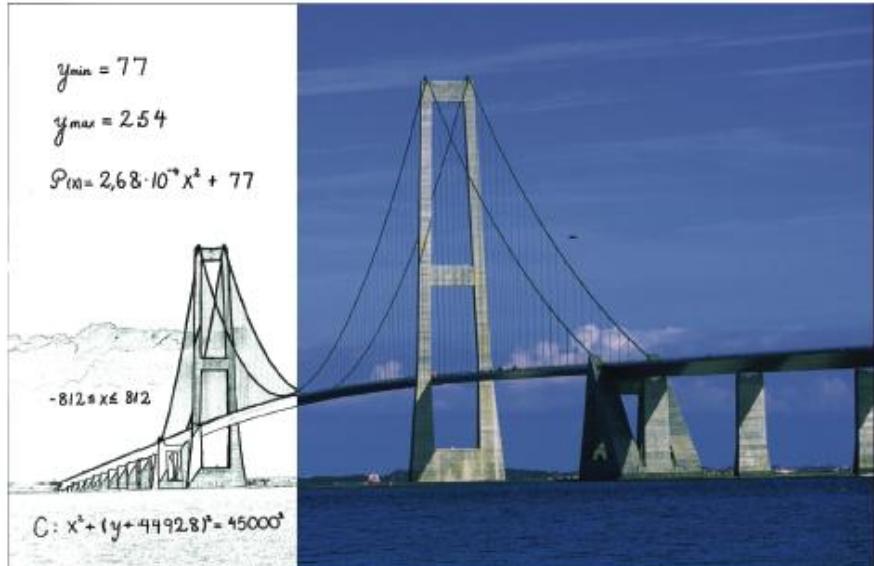
## 1 Introduction

DHI are interested in understanding a rather unusual water extraction system that is operated by a water supply company. Typically when water is extracted from the ground a well is dug and a pump is installed in the well to push the water to the surface where it enters a distribution system of pipes. Such a system may consist of a dozen or so wells each

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## 83. EUROPEAN STUDY GROUP WITH INDUSTRY

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AUGUST 15-19, 2011  
SØNDERBORG, DENMARK

